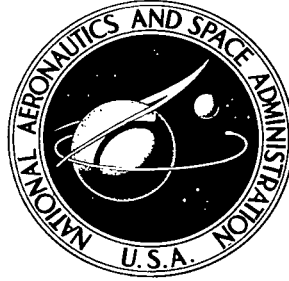


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ELASTIC SCATTERING OF
21-MeV PROTONS FROM NITROGEN 14,
OXYGEN 16, ARGON 40, NICKEL 58,
AND TIN 116

*by**Norton Baron and Regis F. Leonard**Lewis Research Center**and**David A. Lind**University of Colorado*



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ABSTRACT

Differential cross-section angular distributions were measured for 21-MeV incident protons elastically scattered from ^{14}N , ^{16}O , ^{40}Ar , ^{58}Ni , and ^{116}Sn . An optical-model analysis was performed on these data and on previously measured elastic polarizations of 21-MeV incident protons scattered from the same nuclei. The optical potential used in this analysis included a real central term, a surface absorption term, and a real spin-orbit term. Good fits to both the cross sections and polarizations for all nuclei except ^{16}O were obtained by allowing the nine parameters of the optical potential to vary from nucleus to nucleus.

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SUMMARY

Differential cross-section angular distributions were measured for 21-MeV incident protons elastically scattered from nitrogen 14 (^{14}N), oxygen 16 (^{16}O), argon 40 (^{40}Ar), nickel 58 (^{58}Ni), and tin 116 (^{116}Sn). An optical-model analysis was performed on these data and on previously measured elastic polarizations of 21-MeV incident protons scattered from the same nuclei. The optical potential used in this analysis included a real central term, a surface absorption term, and a real spin-orbit term. Good fits to both the cross sections and polarizations for all nuclei except ^{16}O were obtained by allowing the nine parameters of the optical potential to vary from nucleus to nucleus. The diffuseness parameters derived to fit the ^{14}N and ^{16}O data, in general, differed considerably from those derived to fit the scattering from the heavier nuclei. These results were compared with those of two other calculations in which two different sets of nonunique constant-geometric optical-model parameters were assumed, and only the three potential strengths were obtained by searching. As expected, these constant-geometry calculations gave poorer agreement with the data. The disagreement with the polarizations of ^{14}N and ^{16}O was pronounced.

INTRODUCTION

The optical model can reproduce rather well the experimentally measured cross sections and polarizations, provided that the parameters in the optical-model potential are allowed to vary as a function of energy and nucleus (ref. 1). Considerable efforts are being made to find a universal optical-model potential or at least to establish trends in the parameters of the potential with changes in incident proton energy, atomic number, and/or mass number (refs. 2 to 8). In evolving such a potential, data are more useful if they include both cross sections and polarizations measured at the same incident proton energy. Consequently, in this report elastic cross sections for 21-MeV incident protons

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were measured for five nuclei which differ considerably in mass, and for which elastic polarizations at 21 MeV were measured previously (ref. 9). For each nucleus, an optical-model potential was determined which gave the "best fit" to both the cross-section and polarization data.

EXPERIMENTAL ARRANGEMENT

General

The differential cross-section angular distributions of protons elastically scattered from ^{14}N , ^{16}O , ^{40}Ar , ^{58}Ni , and ^{116}Sn were measured by the use of a 21-MeV proton beam extracted from the four-sector, fixed-frequency, alternating-gradient cyclotron at the University of Colorado. After being extracted by electrostatic deflection, the external beam is passed through a 10° steering magnet and two quadrupole lenses, which provide separately for horizontal and vertical focusing. The beam then undergoes a deflection of 30° through a switching magnet and passes into a 91.5-centimeter-diameter scattering chamber through a series of collimators that, in combination with the switching magnet, provide a degree of energy analysis. The detector was mounted on a remotely controlled, motor-driven tray. Similarly, targets were mounted on a remotely controlled, motor-driven table. The detector and target angles were known to $\pm 0.05^\circ$ with respect to the chamber coordinates.

Particle Detection

Reaction product particles were detected by windowless lithium-drifted silicon-semiconductor counters with a compensated depth of 4300 micrometers. These counters, fabricated at the NASA Lewis Research Center (ref. 10), were operated at a temperature of 208 K and at a bias of 400 volts with a leakage current of about 20 nanoamperes. The resolution of these counters, measured with a monoenergetic source of 8.78-MeV alpha particles from polonium 212 (^{212}Po) is typically about 20 keV.

Electronics

The pulse from the detector was fed into a low-noise charge-sensitive preamplifier that was followed by a pulse shaper and further voltage amplification. The amplified pulses were then put into a 4096-channel pulse-height analyzer. The integrated beam

passing through the target was collected in a Faraday cup of conventional design. The total charge collected in the Faraday cup was measured with a low-impedance voltage-to-frequency converter. Its output pulses were stored in the clock channel of the analyzer to give an automatic live-time correction. The spectrum and live-time charge were stored in 256-channel subgroups of the pulse-height analyzer and were dumped, after the accumulation of 16 spectra, onto magnetic tape for subsequent off-line printout.

Beam Energy

The incident beam energy was determined by a kinematic null method (refs. 11 and 12) using the angular dependence of energy for protons scattered from the first excited state of carbon 12 (^{12}C) and from hydrogen. This determination of energy is considered to be accurate to ± 40 keV. The use of the null method on both the left and right sides of the target also determined the incident beam direction to $\pm 0.05^\circ$.

Gas Target

The nitrogen, oxygen, and argon gas targets consisted of an 8.5-centimeter-diameter disk-shaped cell with 6.35-micrometer-thick aluminized polyester-film side windows for the scattered protons and 12.5-micrometer-cobalt-nickel-chromium-alloy windows for the beam entrance and exit. The gas target was designed and constructed at the University of Colorado. The detector telescope consisted of two vertical slits, placed 10 inches (25.4 cm) apart, which defined the target volume and the solid angle. Cross sections were calculated by using only the first-order term in the expression derived by Silverstein (ref. 13).

Energy Resolution

Since the elastically scattered group was well separated from the inelastic groups, there was no need to optimize the resolution. Consequently, a reduction in data-taking time involved widening the incident beam collimating slits to increase the incident beam current. The pulse-height-analyzer resolution was coarse and of the order of 80 keV per channel. The overall energy resolution was approximately 150 keV (full width half maximum).

Cross Sections

Relative cross sections. - Normally enough counts were accumulated in each spectrum so that the standard deviation was less than ± 3 percent. The relative cross sections were always reproducible to within the statistical errors.

Absolute cross sections. - The major sources of probable error in the established scales of absolute cross sections are associated with (1) the determination of the target thickness and (2) the determination of the actual number of incident protons for a given amount of measured charge collection by the Faraday cup.

(1) The accurate determination of the gas target thickness depends primarily on the measurement of the gas pressure. The gas pressure in the target cell was approximately 1 atmosphere and was monitored with an accuracy of ± 0.2 percent. The foil target thickness was determined by accurately weighing a known area of the foil target.

(2) The amount of the 21-MeV incident proton beam that was deflected away from the Faraday cup by multiple scattering in the Havar gas cell windows was estimated to be negligible. Uncertainties in the integrated incident flux were estimated to be less than 1 percent.

When other effects, such as detector efficiency and solid-angle measurement were included, the overall uncertainty in the absolute cross sections was estimated to be less than 5 percent for all the angular distribution measurements reported in this experiment.

EXPERIMENTAL CROSS SECTIONS AND THEIR STATISTICAL ERRORS

Cross sections were obtained for elastic scattering ($5^\circ < \theta_{\text{lab}} < 170^\circ$) of 21-MeV incident protons by gas targets of ^{14}N , ^{16}O , and ^{40}A and by foil targets of ^{58}Ni and ^{116}Sn .

The experimental differential cross sections (in mb/sr) and their associated statistical counting errors (in mb/sr) are listed in the tables on pages 11 to 18 for scattering by ^{14}N , ^{16}O , ^{40}A , ^{58}Ni , and ^{116}Sn . The measured elastic polarizations (ref. 9) are also listed there. These angular distributions, plotted as the ratio to Rutherford scattering, are presented in figures 1(a), 2(a), 3(a), 4(a), and 5(a), respectively.

THE OPTICAL-MODEL POTENTIAL

The optical potential used for the analysis of these scattering data can be written as

$$\begin{aligned}
U(r) = V_c(r) - Vf(r, r_0, a_0) + 4iWa_i \frac{d}{dr} \left[f(r, r_i, a_i) \right] \\
+ \left(\frac{h}{2\pi m_p c} \right)^2 V_{so} \frac{1}{r} \frac{d}{dr} \left[f(r, r_{so}, a_{so}) \right] \vec{l} \cdot \vec{\sigma} \quad (1)
\end{aligned}$$

where $V_c(r)$ is the Coulomb potential between the incident proton and the scattering nucleus, which is assumed to be a uniformly charged sphere of radius

$$R_c = r_c A^{1/3}$$

and has the form

$$\begin{aligned}
V_c(r) &= \frac{ze^2}{2r} \left[3 - \left(\frac{r}{R_c} \right)^2 \right] & r \leq R_c \\
V_c(r) &= \frac{ze^2}{r} & r \geq R_c
\end{aligned}$$

and V and W are the strengths of the real and imaginary parts of the complex central potential and account for the nuclear scattering and absorption, respectively, by the central potential; $f(r)$ denotes the Woods-Saxon radial form factor and has the form

$$f(r) = \left[1 + \exp \left(\frac{r - r_x A^{1/3}}{a_x} \right) \right]^{-1}$$

which is constant in the nuclear interior, falls off in the surface region, and finally drops exponentially to zero. Consequently, the radial derivative of this form factor reaches a maximum in the surface region and makes the imaginary part of the central potential essentially a surface absorption term. In this expression, $r_x A^{1/3}$ measures the overall extent of the potential and is thus a measure of the nuclear radius. The parameter a_x controls the rapidity with which $f(r)$ falls from its maximum value; it is therefore related to the diffuseness of the nuclear surface.

The remaining term in equation (1) is the spin-orbit potential term which is taken proportional to $\vec{l} \cdot \vec{\sigma}$, where \vec{l} and $\vec{\sigma}$ are the angular momentum and Pauli spin,

respectively. For bound particles of negative energy, this spin-dependent term successfully gives the sequence of nuclear states in the shell model. As symmetry requires the spin-orbit forces to be zero in the nuclear interior, the spin-dependent potential may be expected to be small inside the nucleus and appreciable only in the surface region. Consequently, the Thomas form was assumed with the derivative of the Woods-Saxon radial form factor, which has the required surface peaking and a spin-orbit potential strength given by V_{so} .

Volume absorption was not used in this analysis, in accordance with the results of a recent analysis of 18.6-MeV proton cross-section and polarization data (ref. 8).

OPTICAL MODEL ANALYSES OF ^{14}N , ^{16}O , ^{40}A , ^{58}Ni , AND ^{116}Sn

For each of the several nuclei studied, an optical-model analysis was performed to fit simultaneously the polarization and elastic angular distributions. The calculations were performed with an optical-model computer program. The automatic search provision of this program was written by Davidon (ref. 14) and was adapted for use at this Center (unpublished work by Volkin and Giamati of Lewis). The program varies the nine independent parameters of the optical potential to minimize the quantity χ^2/N , which is defined as

$$\frac{\chi^2}{N} = \frac{\sum_{i=1}^{N_\sigma} \left| \frac{\sigma_{\text{exp}}(\theta_i) - \sigma_{\text{calc}}(\theta_i)}{\Delta\sigma_{\text{exp}}(\theta_i)} \right|^2 + \sum_{i=1}^{N_P} \left| \frac{P_{\text{exp}}(\theta_i) - P_{\text{calc}}(\theta_i)}{\Delta P_{\text{exp}}(\theta_i)} \right|^2}{N_\sigma + N_P} \quad (2)$$

where

N_σ	number of experimental data points for cross sections
$\sigma_{\text{exp}}(\theta_i)$	experimentally measured differential cross sections at angle θ_i
$\sigma_{\text{calc}}(\theta_i)$	calculated differential cross sections
$\Delta\sigma_{\text{exp}}(\theta_i)$	experimental uncertainty associated with measured differential cross sections
N_P	number of experimental data points for polarizations
$P_{\text{exp}}(\theta_i)$	experimentally measured differential polarizations at angle θ_i

$P_{\text{calc}}(\theta_i)$ calculated differential polarizations

$\Delta P_{\text{exp}}(\theta_i)$ experimental uncertainty associated with measured differential polarizations

The experimental uncertainties of the cross sections were set equal to 10 percent of the measured cross sections to give a uniform weight to each data point.

A series of calculations was performed for each isotope, whereby the three potential strengths (V, W, and V_{so}) and the three diffusenesses (a_0 , a_i , and a_{so}) were obtained by a six-parameter search. The three radii (r_0 , r_i , and r_{so}), although fixed during each calculation, were varied independently in successive calculations in steps of 0.03 fermi within the limits

$$1.16 \leq r_0 \leq 1.25 \text{ F}$$

$$1.16 \leq r_i \leq 1.25 \text{ F}$$

$$0.99 \leq r_{\text{so}} \leq 1.14 \text{ F}$$

The parametric values that gave the best fit to the experimental data were then used as starting values for a nine-parameter search calculation. The results of these calculations are listed in table I and are shown in figures 1 to 5. Quoted in table I are the quantities χ^2/N , defined by equation (2), and χ_σ^2/N_σ and χ_p^2/N_p , defined by

$$\frac{\chi_\sigma^2}{N_\sigma} = \frac{\sum_{i=1}^{N_\sigma} \left| \frac{\sigma_{\text{exp}}(\theta_i) - \sigma_{\text{calc}}(\theta_i)}{\Delta \sigma_{\text{exp}}(\theta_i)} \right|^2}{N_\sigma} \quad (3)$$

and

$$\frac{\chi_p^2}{N_p} = \frac{\sum_{i=1}^{N_p} \left| \frac{P_{\text{exp}}(\theta_i) - P_{\text{calc}}(\theta_i)}{\Delta P_{\text{exp}}(\theta_i)} \right|^2}{N_p} \quad (4)$$

Guided by the results listed in table I, a number of three-parameter search calculations were performed to determine how well the scattering from these nuclei could be described by using fixed values for all the radii and diffusenesses. The results of one such set of calculations, somewhat typical, are listed in table II and shown in figures 1 to 5 for comparison with the results of the nine-parameter search calculations. Reasonable fits were obtained for all the data except the polarizations of ^{14}N and ^{16}O . Since only five nuclei were studied, there is no intent herein to propose that these particular values of the geometric quantities represent a unique set of average optical-model potential parameters for 21-MeV protons.

For reference, in another series of calculations, the three potential strengths were determined by searching, using the fixed geometry suggested by Perey (ref. 2). The results of these calculations are listed in table III and shown in figures 1 to 5.

DISCUSSION AND CONCLUSIONS

It is only useful to comment on calculations of the differential cross sections and polarizations, because there are no reported measured values of the reaction cross sections for 21-MeV protons for these nuclei. Also, because only five nuclei were studied herein, no statement can be made concerning the dependence of the optical-model potential on an isobaric spin term. The cross sections and polarizations for 21-MeV protons incident on ^{40}A , ^{58}Ni , and ^{116}Sn are well described by a nine-parameter search. The starting values were obtained by previously gridding on the three radii and searching in a six-parameter space of the three potential strengths and diffusenesses. The resultant radii do not differ greatly among these nuclei. Typically, the spin-orbit radius is about 16 percent less than the radius of the real central potential term and is about 25 percent less than the radius of the absorptive potential term. The spin-orbit diffuseness tends to decrease for heavier nuclei, whereas the diffuseness of the real central potential term is relatively constant and is about 0.72 fermi.

The constant geometric parameters suggested by Perey (ref. 2) were determined by an optical-model analysis of 35 different proton angular distributions at five different incident proton energies ranging from 9.4 to 22.2 MeV. The general characteristics of both the polarizations and cross sections are reproduced for each of the three nuclei. However, the values of χ^2/N may be reduced by a factor of 2 to 10 by using a potential derived to fit only the data presented herein, as illustrated in tables II and III.

The optical model is expected to be more successful for heavy- and medium-weight nuclei than for light nuclei, as they more nearly approach the limit of uniform nuclear matter with few isolated resonances to affect the interaction. For lighter nuclei, fluctuations in the parameters are expected to be larger due to differences in nuclear struc-

ture and the smaller density of levels in the compound system. This problem was previously investigated by Daehnick (ref. 15), who analyzed the scattering of 13- to 19-MeV protons by ^{16}O . He observed that the interference of potential scattering with compound nuclear scattering is strong for even 200-keV resolution. Consequently, the application of the optical model to nuclei as light as ^{14}N and ^{16}O is questionable and is illustrated by the results of a nine-parameter search calculation on ^{14}N and ^{16}O . For ^{14}N , the parameters obtained from such a calculation gave a good overall fit, but, in general, the diffuseness parameters differed considerably from those obtained for ^{40}Ar , ^{58}Ni , and ^{116}Sn . The constant geometric parameters listed in tables II and III each give good fits to the ^{14}N cross sections, but the polarization fits are poor. Similarly, for ^{16}O the constant geometric parameters listed in tables II and III result in a poor agreement with the polarization data. However, the quality of fit to these data is considerably improved by the unrestricted nine-parameter-search optical-model calculation.

Lewis Research Center,
National Aeronautics and Space Administration,
Cleveland, Ohio, September 4, 1968,
129-02-04-06-22.

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TABLE I. - RESULTS OF NINE-PARAMETER SEARCH

	Target				
	^{14}N	^{16}O	^{40}A	^{58}Ni	^{116}Sn
Strength of real part of nuclear optical potential, V , MeV	53.3	50.5	50.6	52.2	53.9
Diffuseness of real part of nuclear optical potential, a_0 , F	0.64	0.54	0.717	0.770	0.71
Radius constant of real part of nuclear optical potential, r_0 , F	1.11	1.19	1.17	1.15	1.18
Strength of imaginary part of nuclear optical potential, W , MeV	7.14	9.14	8.25	8.87	10.6
Diffuseness of imaginary part of nuclear optical potential, a_i , F	0.36	0.36	0.676	0.517	0.660
Radius constant of imaginary part of nuclear optical potential, r_i , F	1.40	1.20	1.22	1.33	1.26
Strength of spin-orbit potential, V_{so} , MeV	5.68	2.75	5.64	4.93	5.24
Diffuseness of spin-orbit potential, a_{so} , F	0.34	0.010	0.657	0.535	0.448
Radius constant of spin-orbit potential, r_{so} , F	0.983	0.993	1.01	1.01	1.07
Goodness of fit per data point, χ^2/N	2.08	13.95	3.83	1.93	0.705
Goodness of fit per cross-section data point, χ^2_{σ}/N_P	1.76	3.75	3.26	1.38	0.6
Goodness of fit per polarization data point, χ^2_p/N_P	2.83	34.4	5.26	2.81	0.905
Reaction cross section, σ_R , mb	480	490	1062	1093	1423

TABLE II. - RESULTS OF SEARCH ON POTENTIAL STRENGTHS
(V, W, AND V_{so}) USING SET OF NONUNIQUE
FIXED GEOMETRIC PARAMETERS

	Target				
	$^{14}_N$	$^{16}_O$	$^{40}_A$	$^{58}_{Ni}$	$^{116}_{Sn}$
Strength of real part of nuclear optical potential, V, MeV	48.0	47.2	49.3	49.8	53.7
Diffuseness of real part of nuclear optical potential, a_0 , F	0.70	0.70	0.70	0.70	0.70
Radius constant of real part of nuclear optical potential, r_0 , F	1.19	1.19	1.19	1.19	1.19
Strength of imaginary part of nuclear optical potential, W, MeV	4.37	4.94	8.37	7.08	11.1
Diffuseness of imaginary part of nuclear optical potential, a_i , F	0.64	0.64	0.64	0.64	0.64
Radius constant of imaginary part of nuclear optical potential, r_i , F	1.25	1.25	1.25	1.25	1.25
Strength of spin-orbit potential, V_{so} , MeV	6.02	1.10	4.97	5.18	5.33
Diffuseness of spin-orbit potential, a_{so} , F	0.55	0.55	0.55	0.55	0.55
Radius constant of spin-orbit potential, r_{so} , F	1.05	1.05	1.05	1.05	1.05
Goodness of fit per data point, χ^2/N	5.89	38.0	4.14	3.62	0.968
Goodness of fit per cross-section data point, χ^2/N_σ	1.78	5.52	3.18	1.70	0.775
Goodness of fit per polarization data point, χ^2/N_P	16.3	103	6.28	6.72	1.33
Reaction cross section, σ_R , mb	528	597	1047	1084	1392

TABLE III. - RESULTS OF SEARCH ON POTENTIAL STRENGTHS

(V, W, AND V_{so}) USING SET OF FIXED GEOMETRICPARAMETERS SUGGESTED BY PEREY^a

	Target				
	$^{14}_N$	$^{16}_O$	$^{40}_A$	$^{58}_{Ni}$	$^{116}_{Sn}$
Strength of real part of nuclear optical potential, V, MeV	45.6	44.5	45.3	47.9	49.5
Diffuseness of real part of nuclear optical potential, a_0 , F	0.65	0.65	0.65	0.65	0.65
Radius constant of real part of nuclear optical potential, r_0 , F	1.25	1.25	1.25	1.25	1.25
Strength of imaginary part of nuclear optical potential, W, MeV	6.09	6.66	10.7	9.51	14.7
Diffuseness of imaginary part of nuclear optical potential, a_i , F	0.47	0.47	0.47	0.47	0.47
Radius constant of imaginary part of nuclear optical potential, r_i , F	1.25	1.25	1.25	1.25	1.25
Strength of spin-orbit potential, V_{so} , MeV	7.02	0.987	3.48	4.97	5.74
Diffuseness of spin-orbit potential, a_{so} , F	0.65	0.65	0.65	0.65	0.65
Radius constant of spin-orbit potential, r_{so} , F	1.25	1.25	1.25	1.25	1.25
Goodness of fit per data point, χ^2/N	5.95	38.4	8.90	9.52	8.26
Goodness of fit per cross-section data point, $\chi^2_{\sigma}/N_{\sigma}$	1.08	5.21	6.23	5.32	6.18
Goodness of fit per polarization data point, χ^2_p/N_p	18.3	105	14.8	16.3	12.2
Reaction cross section, σ_R , mb	495	551	944	995	1253

^aRef. 2.

TABLE VIII. - DIFFERENTIAL CROSS SECTIONS FOR SCATTERING OF 21-MeV

PROTONS BY TIN 116

[Incident proton energy for cross section measurements, 21.3 MeV; incident proton energy for polarization measurements, 20.8 MeV.]

Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization	Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization
10.09	1.24×10^5	3.56×10^2	-----	-----	90.5	6.64	5.37×10^{-2}	0.405	0.049
15.13	2.06×10^4	5.62×10^1	0.038	0.025	95.5	8.50	1.20×10^{-1}	-----	-----
20.17	6.63×10^3	2.53×10^1	-----	-----	98.0	-----	-----	-.109	.050
22.7	-----	-----	0	.035	100.49	8.40	1.36×10^{-1}	-----	-----
25.21	2.84×10^3	2.37×10^1	-----	-----	105.48	6.19	8.66×10^{-2}	-.309	.048
30.25	1.13×10^3	6.58	-.024	.066	110.47	3.74	3.38×10^{-2}	-----	-----
35.29	4.16×10^2	1.99	-----	-----	113.0	-----	-----	-.677	.067
37.8	-----	-----	-.130	.025	115.45	1.57	2.52×10^{-2}	-----	-----
40.32	1.76×10^2	1.14	-----	-----	117.94	1.10	3.02×10^{-2}	-----	-----
45.35	8.73×10^1	6.48×10^{-1}	.017	.039	120.43	8.85×10^{-1}	1.61×10^{-2}	.525	.091
47.87	7.26×10^1	3.80×10^{-1}	-----	-----	122.92	1.04	2.97×10^{-2}	-----	-----
50.38	6.70×10^1	3.56×10^{-1}	-----	-----	125.41	1.27	1.73×10^{-2}	-----	-----
52.9	6.42×10^1	3.59×10^{-1}	.315	.046	127.9	-----	-----	.562	.077
55.41	6.58×10^1	5.77×10^{-1}	-----	-----	130.38	2.07	3.32×10^{-2}	-----	-----
57.92	6.09×10^1	3.50×10^{-1}	-----	-----	135.35	2.58	3.53×10^{-2}	.228	.071
60.43	5.84×10^1	5.26×10^{-1}	-.006	.050	140.32	2.43	3.79×10^{-2}	-----	-----
65.45	4.58×10^1	4.26×10^{-1}	-----	-----	142.8	-----	-----	-.087	.078
68.0	-----	-----	-.251	.040	145.29	2.05	4.86×10^{-2}	-----	-----
70.47	2.77×10^1	1.61×10^{-1}	-----	-----	150.25	1.59	2.02×10^{-2}	-.553	.085
75.48	1.29×10^1	1.28×10^{-1}	-.581	.057	155.21	1.32	3.70×10^{-2}	-----	-----
80.49	5.04	4.20×10^{-2}	-----	-----	157.7	-----	-----	-.245	.077
82.99	4.11	5.84×10^{-2}	.368	.068	160.17	1.35	3.73×10^{-2}	-----	-----
85.50	4.29	4.38×10^{-2}	-----	-----	165.13	-----	-----	.352	.081
88.0	5.46	6.71×10^{-2}	-----	-----					

TABLE IV. - DIFFERENTIAL CROSS SECTIONS FOR SCATTERING OF 21-MeV

PROTONS BY NITROGEN 14

[Incident proton energy for cross section measurements, 21.02 MeV; incident proton energy for polarization measurements, 20.8 MeV.]

Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization	Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization
5.25	4.47×10^4	1.50×10^2	-----	-----	83.95	2.82×10^1	3.19×10^{-1}	-----	-----
6.32	1.84×10^4	1.57×10^2	-----	-----	86.7	-----	-----	0.173	0.044
8.46	5.04×10^3	2.47×10^1	-----	-----	88.99	2.16×10^1	2.83×10^{-1}	-----	-----
9.53	3.48×10^3	2.52×10^1	-----	-----	94.01	1.64×10^1	2.28×10^{-1}	-----	-----
10.6	2.33×10^3	1.43×10^1	-----	-----	94.2	-----	-----	.152	.058
11.68	2.00×10^3	1.40×10^1	-----	-----	98.99	1.15×10^1	1.78×10^{-1}	-----	-----
12.75	1.62×10^3	1.34×10^1	-----	-----	101.8	-----	-----	-.059	.074
13.82	1.40×10^3	1.04×10^1	-----	-----	103.94	7.90	1.61×10^{-1}	-----	-----
14.89	1.28×10^3	8.22	-----	-----	108.86	5.22	9.30×10^{-2}	-----	-----
15.96	1.16×10^3	8.27	-----	-----	109.1	-----	-----	.007	.069
17.03	1.03×10^3	3.77	-----	-----	113.76	4.27	8.20×10^{-2}	-----	-----
19.16	8.98×10^2	3.58	-----	-----	116.4	-----	-----	-.077	.086
21.3	7.97×10^2	5.03	-----	-----	118.62	3.64	6.49×10^{-2}	-----	-----
23.43	6.81×10^2	3.54	-----	-----	123.45	3.58	7.89×10^{-2}	-----	-----
25.57	5.79×10^2	4.55	-----	-----	123.7	-----	-----	.321	.092
27.70	4.80×10^2	1.76	-----	-----	128.26	3.9	6.98×10^{-2}	-----	-----
29.82	3.97×10^2	1.55	-----	-----	130.8	-----	-----	.589	.073
31.95	3.22×10^2	1.52	-----	-----	133.04	4.09	5.50×10^{-2}	-----	-----
37.25	1.81×10^2	8.78×10^{-1}	-----	-----	137.79	4.25	6.89×10^{-2}	-----	-----
40.1	-----	-----	-0.367	0.028	138.0	-----	-----	.773	.070
42.54	9.44×10^1	8.62×10^{-1}	-----	-----	142.53	4.48	7.66×10^{-2}	-----	-----
47.8	4.54×10^1	4.21×10^{-1}	-.464	.043	145.1	-----	-----	.872	.071
53.05	2.84×10^1	4.34×10^{-1}	-----	-----	147.24	4.47	7.44×10^{-2}	-----	-----
55.8	-----	-----	-.105	.051	151.94	4.49	5.12×10^{-2}	-----	-----
58.27	2.63×10^1	2.58×10^{-1}	-----	-----	152.2	-----	-----	.791	.066
63.46	3.01×10^1	2.84×10^{-1}	-----	-----	156.62	4.34	7.64×10^{-2}	-----	-----
63.7	-----	-----	.187	.057	159.1	-----	-----	.581	.055
68.62	3.35×10^1	3.36×10^{-1}	-----	-----	161.28	4.43	6.07×10^{-2}	-----	-----
71.4	-----	-----	.245	.051	165.94	4.38	4.81×10^{-2}	-----	-----
73.76	3.55×10^1	3.84×10^{-1}	-----	-----	166.1	-----	-----	.506	.055
78.87	3.27×10^1	3.60×10^{-1}	-----	-----	170.59	4.21	6.95×10^{-2}	-----	-----
79.1	-----	-----	.197	.058					

TABLE V. - DIFFERENTIAL CROSS SECTIONS FOR SCATTERING OF 21-MeV

PROTONS BY OXYGEN 16

[Incident proton energy for cross section measurements, 20.93 MeV; incident proton energy for polarization measurements 20.7 MeV.]

Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization	Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization
5.19	6.02×10^4	1.18×10^2	-----	-----	68.36	3.56×10^1	3.59×10^{-1}	-----	-----
6.25	2.39×10^4	6.53×10^1	-----	-----	70.92	3.76×10^1	4.08×10^{-1}	-0.183	.05
8.38	6.55×10^3	4.04×10^1	-----	-----	73.48	3.71×10^1	3.69×10^{-1}	-.121	.01
10.5	3.00×10^3	2.37×10^1	-----	-----	78.58	3.59×10^1	3.47×10^{-1}	-.371	.054
12.63	1.88×10^3	1.40×10^1	-----	-----	83.65	2.97×10^1	3.36×10^{-1}	-----	-----
12.84	1.73×10^3	8.35	-----	-----	86.1	-----	-----	-.307	.043
15.96	1.35×10^3	7.35	-----	-----	88.69	2.47×10^1	2.95×10^{-1}	-.288	.012
17.08	1.11×10^3	4.65	-----	-----	93.70	1.75×10^1	2.26×10^{-1}	-.424	.054
19.20	9.40×10^2	4.50	-----	-----	98.69	1.21×10^1	2.12×10^{-1}	-----	-----
21.32	7.91×10^2	3.62	-----	-----	101.1	-----	-----	-.502	.074
23.44	6.68×10^2	3.33	-----	-----	103.65	7.73	1.67×10^{-1}	-.452	.021
25.55	5.71×10^2	3.07	-----	-----	108.58	5.06	1.34×10^{-1}	-.434	.073
26.61	4.69×10^2	2.22	-----	-----	113.49	3.31	1.08×10^{-1}	-----	-----
31.68	2.99×10^2	3.07	-----	-----	115.8	-----	-----	-.344	.089
31.89	2.97×10^2	1.92	-----	-----	118.37	2.85	9.00×10^{-2}	-.170	.033
37.16	1.64×10^2	1.23	-----	-----	123.22	2.67	9.38×10^{-2}	.062	.089
39.70	-----	-----	-0.441	0.031	128.95	2.78	8.53×10^{-2}	-----	-----
42.41	7.71×10^1	6.32×10^{-1}	-----	-----	130.3	-----	-----	.344	.081
47.30	-----	-----	-.531	.041	132.86	2.76	9.06×10^{-2}	.460	.029
47.43	3.47×10^1	5.37×10^{-1}	-----	-----	137.44	2.61	3.86×10^{-2}	.590	.074
47.64	3.58×10^1	3.23×10^{-1}	-----	-----	137.65	2.57	8.43×10^{-2}	-----	-----
52.85	2.31×10^1	2.26×10^{-1}	-----	-----	142.42	2.69	8.25×10^{-2}	-----	-----
54.93	2.27×10^1	2.12×10^{-1}	-----	-----	144.7	-----	-----	.700	.072
55.30	-----	-----	.034	.049	146.96	2.73	5.33×10^{-2}	-----	-----
57.01	2.45×10^1	4.32×10^{-1}	-----	-----	147.17	2.87	8.09×10^{-2}	-----	-----
58.05	-----	-----	.002	.01	151.90	3.29	8.67×10^{-2}	.858	.069
60.12	2.75×10^1	3.22×10^{-1}	-----	-----	156.62	3.87	8.11×10^{-2}	-----	-----
63.10	-----	-----	.023	.052	158.9	-----	-----	.751	.062
63.22	3.09×10^1	2.89×10^{-1}	-----	-----	161.33	4.55	1.02×10^{-1}	-----	-----
65.79	3.48×10^1	4.39×10^{-1}	-----	-----	165.82	-----	-----	.498	.053
68.15	3.39×10^1	5.54×10^{-1}	-----	-----					

TABLE VI. - DIFFERENTIAL CROSS SECTIONS FOR SCATTERING OF 21-MeV

PROTONS BY ARGON 40

[Incident proton energy for cross section measurements, 21.13 MeV; incident proton energy for polarization measurements, 21.0 MeV.]

Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization	Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization
5.0	3.22×10^5	9.42×10^2	-----	-----	76.40	-----	-----	0.225	0.158
6.02	1.30×10^5	5.50×10^2	-----	-----	81.29	6.72×10^1	1.64×10^{-1}	-----	-----
8.07	3.28×10^4	2.50×10^2	-----	-----	83.90	-----	-----	.285	.124
10.12	1.15×10^4	1.15×10^2	-----	-----	86.31	9.60	2.23×10^{-1}	-----	-----
12.17	5.79×10^3	2.35×10^1	-----	-----	91.32	1.09×10^1	2.53×10^{-1}	.326	.123
14.22	3.36×10^3	1.21×10^1	-----	-----	96.31	1.06×10^1	2.35×10^{-1}	-----	-----
16.27	2.17×10^3	8.04	-----	-----	98.90	-----	-----	-.050	.138
18.32	1.53×10^3	1.07×10^1	-----	-----	101.29	8.83	2.73×10^{-1}	-----	-----
20.37	1.06×10^3	6.33	-----	-----	106.27	6.64	1.93×10^{-1}	-----	-----
22.41	7.46×10^2	3.83	-----	-----	106.4	-----	-----	-.066	.072
24.46	5.14×10^2	3.07	-----	-----	111.23	3.83	1.21×10^{-1}	-----	-----
26.51	3.49×10^2	2.20	-----	-----	113.8	-----	-----	-.040	.077
28.55	2.29×10^2	1.91	-----	-----	116.18	2.47	7.72×10^{-2}	-----	-----
30.60	1.46×10^2	9.73×10^{-1}	-----	-----	121.12	1.53	7.11×10^{-2}	.482	.098
35.70	1.55×10^1	2.71×10^{-1}	-----	-----	126.05	1.05	4.70×10^{-2}	-----	-----
38.40	-----	-----	0.754	0.099	128.6	-----	-----	.852	.101
40.80	3.64×10^1	3.96×10^{-1}	-----	-----	130.98	1.02	5.08×10^{-2}	-----	-----
45.89	7.03×10^1	7.21×10^{-1}	-----	-----	135.89	1.39	4.82×10^{-2}	.405	.129
46.0	-----	-----	.260	.085	140.8	1.72	5.65×10^{-2}	-----	-----
50.98	8.28×10^1	6.88×10^{-1}	-----	-----	143.4	-----	-----	.280	.072
53.60	-----	-----	-.209	.092	150.59	2.05	5.56×10^{-2}	-.057	.105
56.06	7.11×10^1	7.03×10^{-1}	-----	-----	155.48	1.61	5.35×10^{-2}	-----	-----
61.12	4.65×10^1	4.84×10^{-1}	-.494	.066	158.1	-----	-----	.716	.089
66.18	2.31×10^1	3.21×10^{-1}	-----	-----	160.36	1.19	4.23×10^{-2}	-----	-----
68.8	-----	-----	-.467	.112	165.24	.88	2.15×10^{-2}	-----	-----
71.23	1.02×10^1	2.03×10^{-1}	-----	-----	165.4	-----	-----	.488	.108
76.27	5.87	1.81×10^{-1}	-----	-----					

TABLE VII. - DIFFERENTIAL CROSS SECTIONS FOR SCATTERING OF 21-MeV

PROTONS BY NICKEL 58

[Incident proton energy for cross section measurements, 21.3 MeV; incident proton energy for polarization measurements, 20.9 MeV.]

Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization	Center-of-mass scattering angle, θ_{cm} , deg	Differential cross section, $d\sigma/d\Omega$, mb/sr	Statistical error of differential cross section, $\pm\Delta d\sigma/d\Omega$, mb/sr	Polarization, P	$\pm\Delta$ Polarization
10.17	3.68×10^4	7.37×10^1	-----	-----	85.99	1.90×10^1	9.14×10^{-2}	-----	-----
15.26	5.03×10^3	9.51	-0.017	0.009	91.00	1.51×10^1	6.10×10^{-2}	-0.215	0.044
20.34	1.50×10^3	4.72	-----	-----	95.99	9.30	6.78×10^{-2}	-----	-----
22.9	-----	-----	-.110	.021	98.5	-----	-----	-.597	.067
25.42	5.41×10^2	2.54	-----	-----	100.98	4.80	4.67×10^{-2}	-----	-----
30.5	1.99×10^2	1.22	.096	.045	105.96	2.59	3.27×10^{-2}	-.297	.069
35.57	1.22×10^2	7.30×10^{-1}	-----	-----	107.95	2.37	3.06×10^{-2}	-----	-----
36.59	1.18×10^2	5.62×10^{-1}	-----	-----	110.94	2.66	3.51×10^{-2}	-----	-----
38.1	-----	-----	.186	.039	113.4	-----	-----	.600	.065
38.61	1.18×10^2	7.35×10^{-1}	-----	-----	115.9	3.62	4.75×10^{-2}	-----	-----
40.64	1.21×10^2	8.34×10^{-1}	-----	-----	120.86	4.25	4.06×10^{-2}	.592	.064
45.70	1.19×10^2	6.78×10^{-1}	-.091	.037	125.82	4.49	6.19×10^{-2}	-----	-----
50.76	8.98×10^1	3.49×10^{-1}	-----	-----	128.3	-----	-----	.569	.071
53.3	-----	-----	-.347	.050	130.76	4.19	5.49×10^{-2}	-----	-----
55.82	5.23×10^1	5.27×10^{-1}	-----	-----	135.70	3.67	5.36×10^{-2}	.008	.075
60.86	2.08×10^1	1.12×10^{-1}	-.735	.058	140.64	3.43	2.95×10^{-2}	-----	-----
64.90	7.24	6.39×10^{-2}	-----	-----	143.1	-----	-----	-.371	.083
65.90	5.58	5.64×10^{-2}	-----	-----	145.57	3.30	4.29×10^{-2}	-----	-----
66.91	4.62	4.54×10^{-2}	-----	-----	150.50	3.44	4.47×10^{-2}	-.130	.079
68.92	4.17	4.17×10^{-2}	.115	.077	155.42	3.48	4.39×10^{-2}	-----	-----
70.94	5.50	3.30×10^{-2}	-----	-----	157.9	-----	-----	.327	.075
75.96	1.22×10^1	1.15×10^{-1}	.389	.055	160.34	3.20	4.23×10^{-2}	-----	-----
80.98	1.89×10^1	1.36×10^{-1}	-----	-----	165.26	-----	-----	.592	.077
83.4	-----	-----	.092	.037					

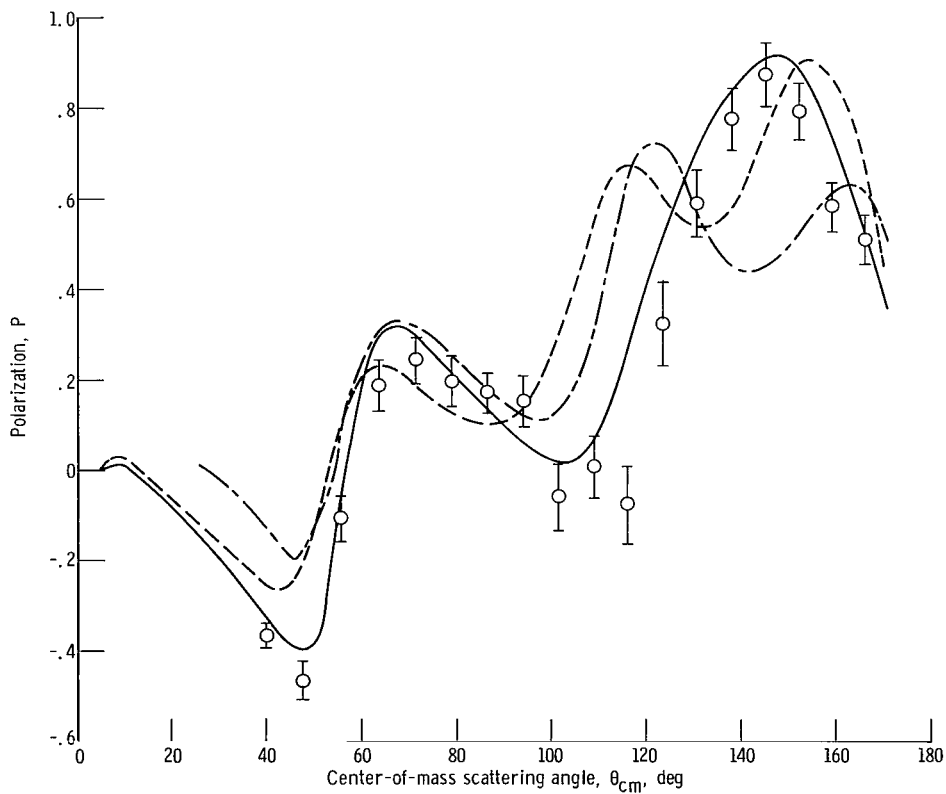
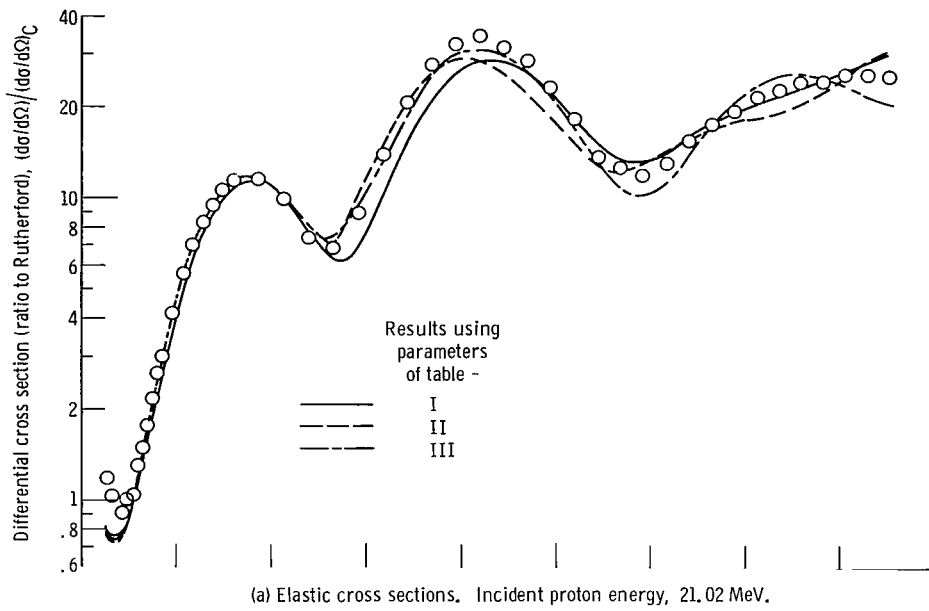


Figure 1. - Experimental and theoretical cross sections and polarizations for elastic scattering from nitrogen 14 of 21-MeV protons.

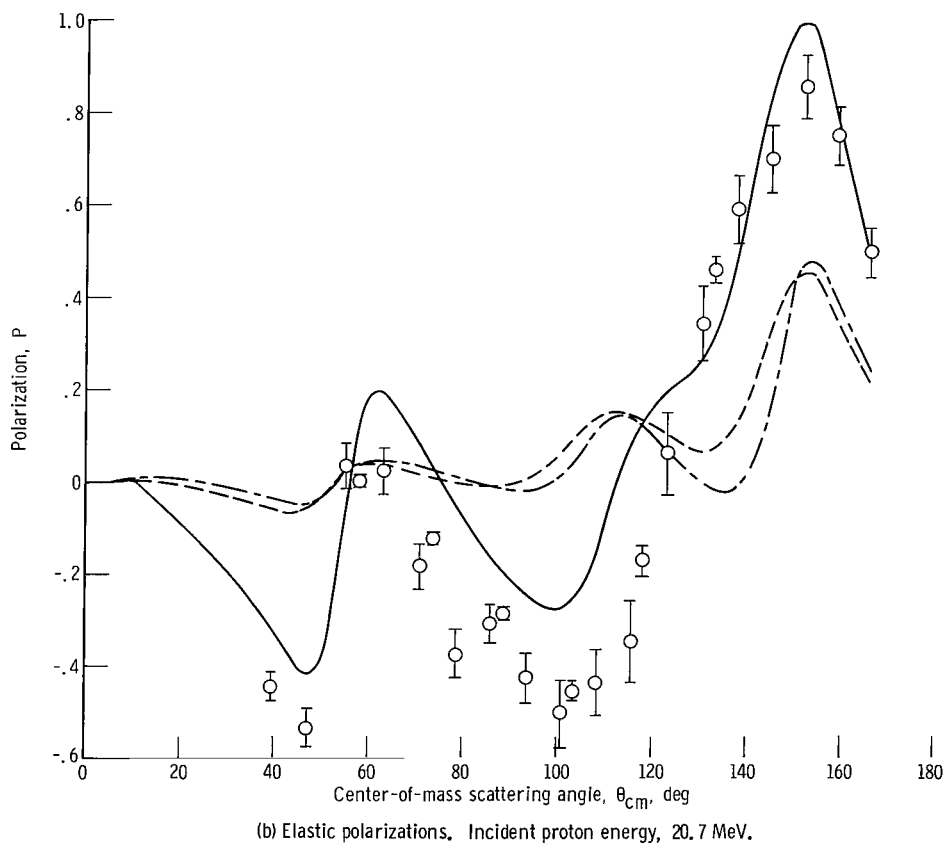
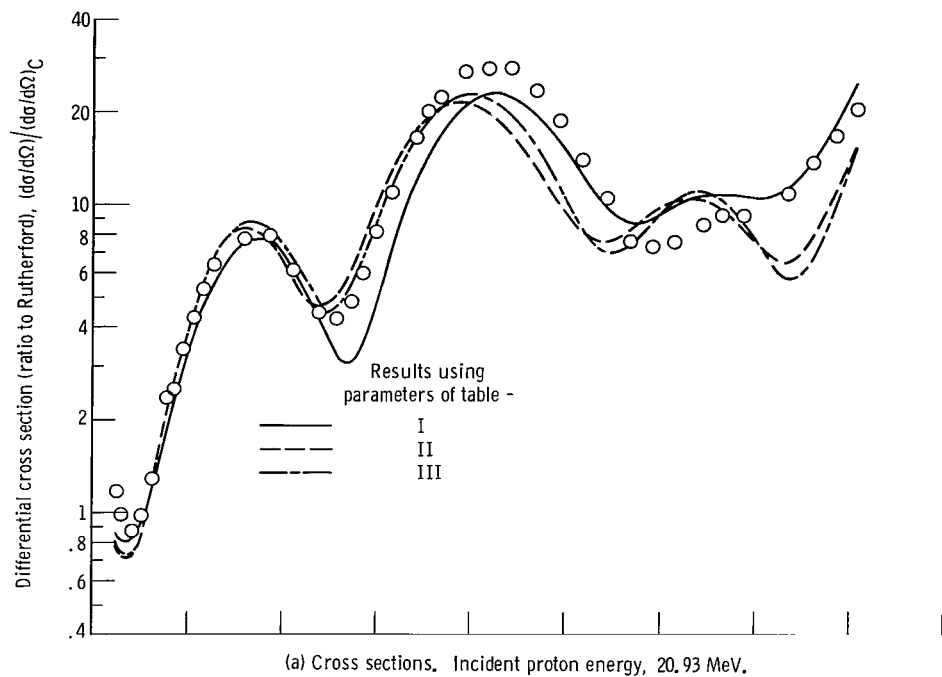


Figure 2. - Experimental and theoretical cross sections and polarizations for elastic scattering from oxygen 16 of 21-MeV protons.

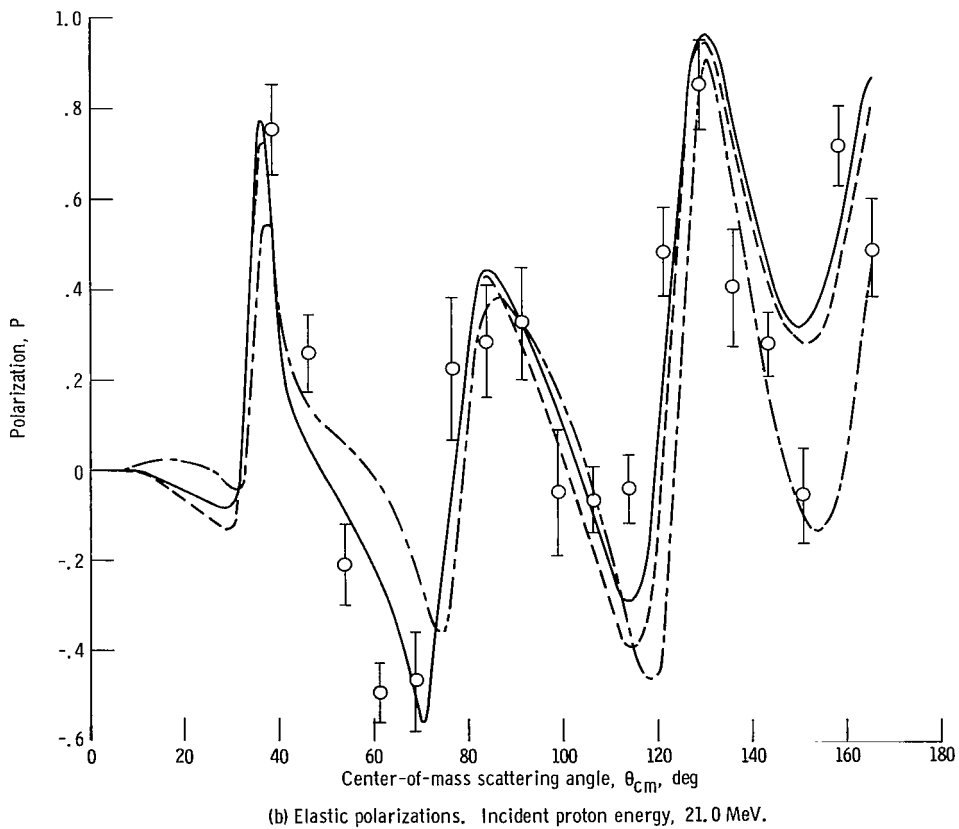
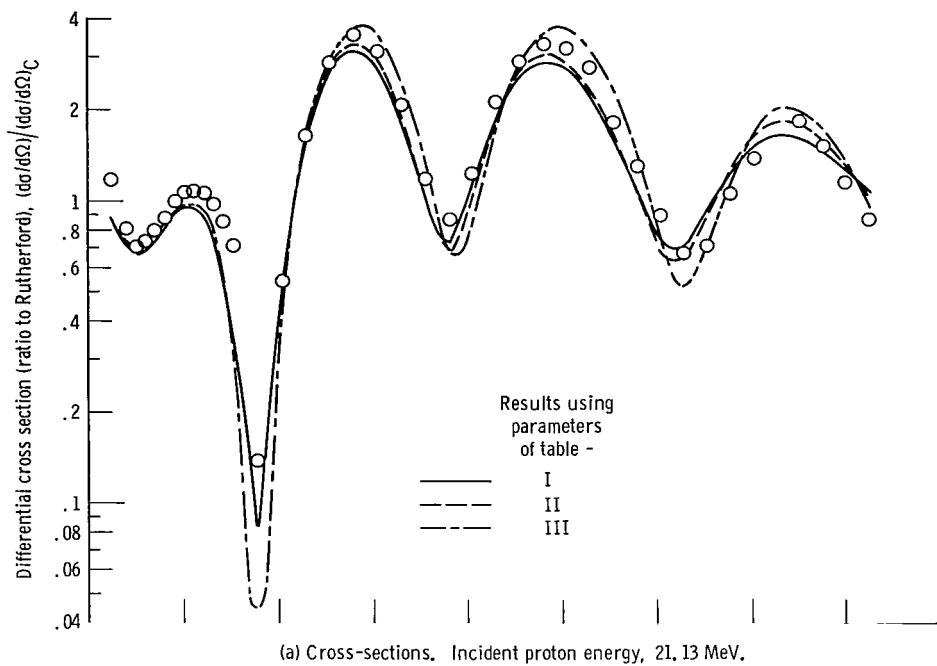


Figure 3. - Experimental and theoretical cross sections and polarizations for elastic scattering from argon 40 of 21-MeV protons.

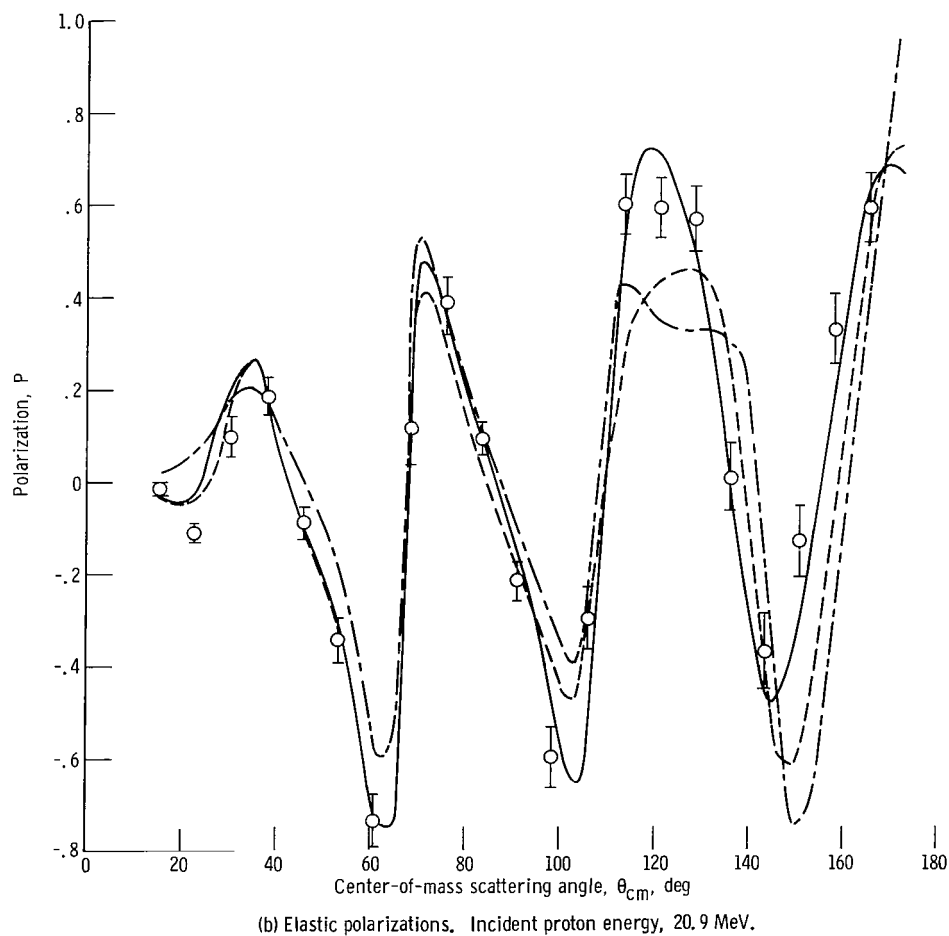
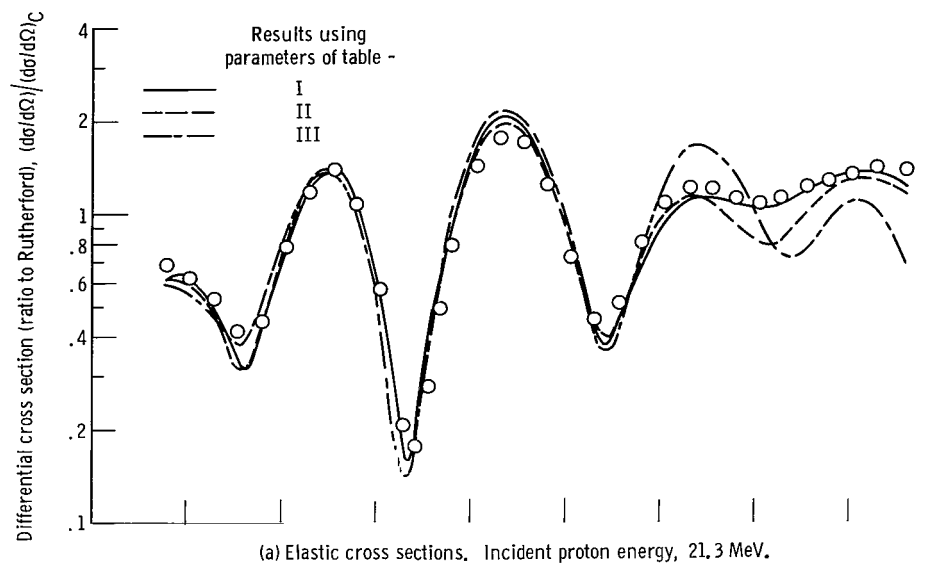


Figure 4. - Experimental and theoretical cross sections and polarizations for elastic scattering from nickel 58 of 21-MeV protons.

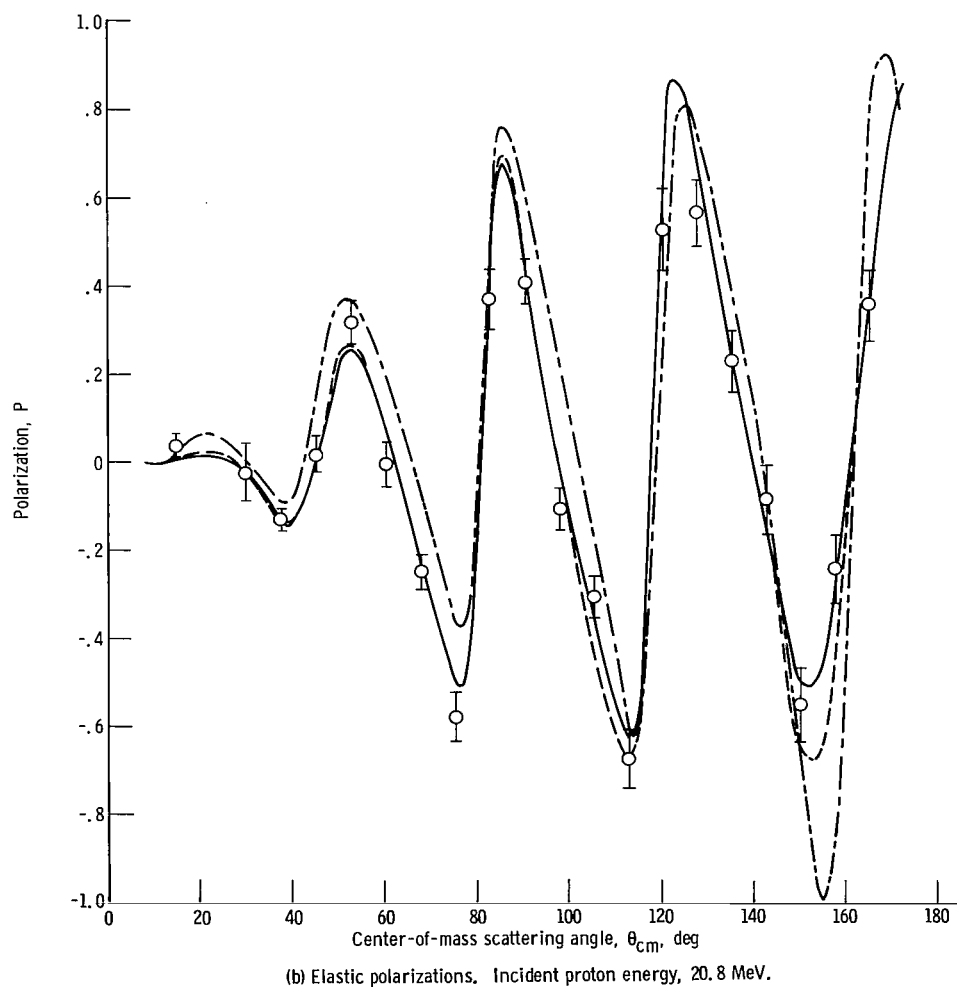
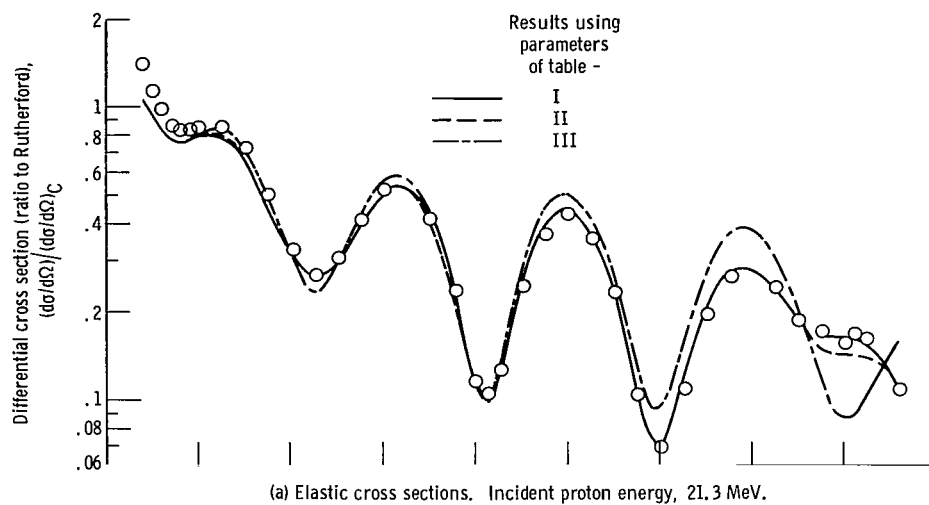


Figure 5. - Experimental and theoretical cross sections and polarizations for elastic scattering from tin 116 of 21-MeV protons.

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